GCSE Maths - Probability

# Enumeration, Venn Diagrams, Tree Diagrams and Tables 

Worksheet



This worksheet will show you how to work out different types of enumeration questions. Each section contains a worked example, a question with hints and then questions for you to work through on your own.

## Section A

## Worked Example

Jason has 4 counters in a bag. One counter is red (R), one is blue (B), one is green ( $G$ ) and one is yellow (Y). He draws the counters from the bag one at a time. In how many different orders could he draw the counters?

Step 1: Use systematic listing to work through each combination.
Start by fixing one of the items in position 1 and another in position 2. Then swap the last two items in positions 3 and 4 to produce the first two combinations. Then, change the second item and swap the last two items again. Continue until you have found all combinations relating to the fixed first position item.
$Y G B R$
$Y G R B$
$Y R G B$
$Y R B G$
$Y B G R$
$Y B R G$

Step 2: Consider another item in position 1. Work through each possibility, swapping the numbers until you have tried every combination of numbers in every position.

| $G Y R B$ | $R G Y B$ | $B G R Y$ |
| :--- | :--- | :--- |
| $G Y B R$ | $R G B Y$ | $B G Y R$ |
| $G B Y R$ | $R B Y G$ | $B Y R G$ |
| $G B R Y$ | $R B G Y$ | $B Y G R$ |
| $G R B Y$ | $R Y G B$ | $B R G Y$ |
| $G R Y B$ | $R Y B G$ | $B R Y G$ |

Step 3: Count the number of combinations you have found. Double check that you have not repeated any combinations.

There are 6 combinations in the first column. You could use this, and the fact that there are 4 colours of counter, to work out that the total number of combinations is:

$$
6 \times 4=24 \text { combinations of counters }
$$

## Guided Example

In a sandwich shop there are 2 kinds of bread, 3 fillings and 4 drinks to choose from. How many different meal deals can be made?

Step 1: List or calculate the possible combinations.
You could use the product rule for this question because there are a lot of variables to consider listing.

Now it's your turn!
If you get stuck, look back at the worked and guided examples.

1. Janae has 4 shirts, 2 pairs of jeans and 2 pairs of shoes. How many outfits can she make?
2. Louis is going to have a meal. He can choose one main and one dessert from the menu. Write down all the possible combinations that Louis could choose.

| Menu |  |
| :---: | :---: |
| Main | Dessert |
| Soup | Ice Cream |
| Pasta | Cheesecake |
| Pizza | Tiramisu |

3. Maia flips a coin and rolls a 6-sided die. Use the following table to help list all the possible outcomes.

|  |  | Die |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |  |  |
| Coin | Heads |  |  |  |  |  |  |  |

4. Justin has a bag containing red, green and blue counters. He picks three counters from the bag one at a time. Draw a tree diagram to show the possible combinations of counters that he could choose.

## Section B

## Worked Example

A school has $\mathbf{2 0 0}$ students. There are $\mathbf{8 0}$ students in the French class ( F ). There are 60 students in the Spanish class ( S ). Twenty students study both languages.
Complete the Venn diagram to show this information.


Step 1: Work out how many students study both languages and write this in the intersection of the circles.

20 students study both languages.


Step 2: Calculate the number of students who study just French or just Spanish.
80 students study French, but 20 of them study French AND Spanish:

80-20 $=60$ students study just French.
60 students study Spanish, but 20 of them study French AND Spanish:
$60-20=40$ students study just Spanish.


Step 3: Calculate the number of students who do not study a language. Write this number outside of the circles.
$60+20+40=120$ students study a language
200-120 = 80 students do not study a language


## Guided Example

## Consider the set of data values

$D=\{2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18\}$.
Let $A=$ multiples of 3
Let $B=$ multiples of 4 .
Complete the Venn diagram for the set D .


Step 1: For each number in the set, decide which numbers are a multiple of 3 and a multiple of 4. Write these numbers in the intersection of $A$ and $B$.

Step 2: Write the remaining multiples of 3 and 4 in the correct circles.

Step 3: Write the numbers that are neither multiples of 3 nor 4 in the correct section of the Venn diagram.

## Now it's your turn!

If you get stuck, look back at the worked and guided examples.
5. Here is a Venn diagram. Write down the letters that are in:
a) $A$
b) $A^{\prime}$

c) $A \cap B$
6. There are 60 members in an athletics club.

9 athletes do long jump and hammer throw.
20 athletes do only long jump.
14 athletes do not do long jump or hammer throw.

Complete the Venn diagram. How many athletes only do hammer throw?


## Section C

## Worked Example

The Venn diagram below shows whether students passed their Maths and English exams. A student is chosen at random. Find the probability that they passed Maths and English.


Step 1: Find the population total.
There are 15 students who did not pass either exam and 50 students who passed both. There are also 15 students who passed only Maths, and 20 students who passed only English.

$$
15+50+15+20=100 \text { students }
$$

Step 2: Find the number of students in the target space.
We are trying to find $P(M \cap E)$. This means we need to look at the intersection between Maths and English.

There are 50 students in the intersection.

Step 3: Calculate the probability.

$$
\operatorname{Probability}(M \cap E)=\frac{50}{100}=\frac{1}{2}
$$

Guided Example
Using the Venn Diagram, find $P\left(A^{\prime}\right)$.
Step 1: Find the population total.

Step 2: Find the number in the target space A'


Step 3: Calculate the required probability.

If you get stuck, look back at the worked and guided examples.
7. Shade the given areas:
a) A

b) $\mathrm{B}^{\prime}$

c) $A \cap B$

d) $A^{\prime} \cap B^{\prime}$

8. From the Venn diagram, find the following probabilities:

a) $\mathrm{P}(\mathrm{A})$
b) $P\left(B^{\prime}\right)$
c) $P(A \cap B)$
d) $P\left(A^{\prime} \cup B\right)$
e) $P\left((A \cap B)^{\prime}\right)$
9. Juliana goes to the local leisure centre. She records that 50 people visit that day. Of those that visit,

30 visited the gym
13 people went swimming
22 people went to the spa
6 people went swimming and went to the spa
11 people went to the spa and visited the gym
12 people went swimming and visited the gym 5 people went swimming, visited the gym and went to the spa
a) Draw a Venn diagram to display this information.
b) How many people visited the leisure centre but did not visit any of the gym, spar or swimming pool?
c) One person is picked at. What is the probability that they visited the gym and went swimming?

